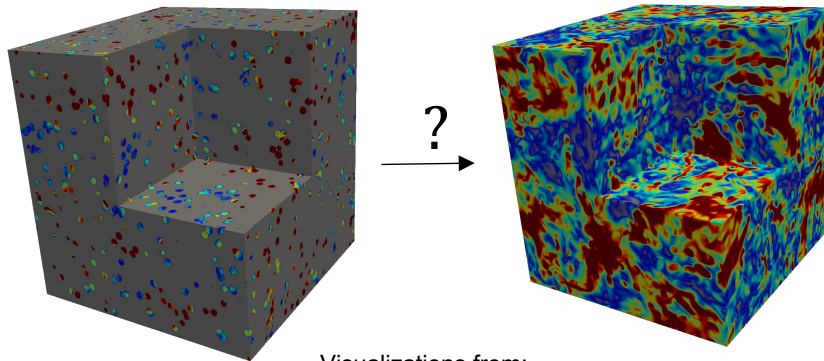


# Classifying Turbulent Environments via Machine Learning

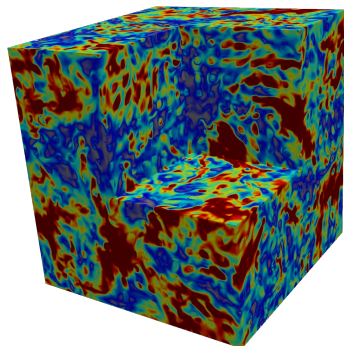


APS DFD 2022  
75<sup>th</sup> Annual Meeting  
November 20 - 22, 2022  
Indianapolis



Visualizations from:

Di Leoni, P. C., Mazzino, A., & Biferale, L. (2020). Physical Review X, 10(1), 011023.



?  $\rightarrow \frac{d\mathbf{u}}{dt}$

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**CREDITS:** L. Biferale (Uni. Tor Vergata, IT),  
F. Bonaccorso (Uni. Tor Vergata, IT), P. Clark di  
Leoni (Uni. of Buenos Aires, ARG)



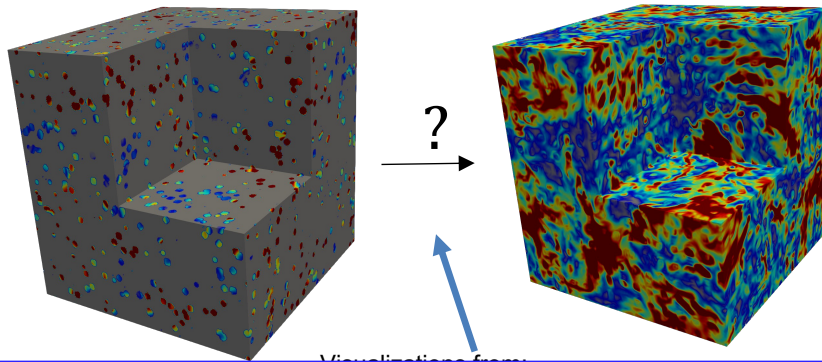
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# Classifying Turbulent Environments via Machine Learning



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**Michele Buzzicotti**

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[Data reconstruction of turbulent flows with Gappy POD and Generative Adversarial Networks](#) T. Li, M. Buzzicotti, F. Bonaccorso, L. Biferale, M. Wan and S. Chen *arXiv preprint arXiv:2210.11921* (Submitted to JOT)

[Reconstructing Rayleigh–Bénard flows out of temperature-only measurements using nudging](#) L Agasthya, P Clark Di Leoni, L Biferale *Physics of Fluids* 34 (1), 015128

[Reconstruction of turbulent data with deep generative models for semantic inpainting from TURB-Rot database](#) M Buzzicotti, F Bonaccorso, PC Di Leoni, L Biferale *Physical Review Fluids* 6 (5), 050503

[ma2.infn.it](mailto:m.buzzicotti@roma2.infn.it)

Tor Vergata, IT),  
ta, IT), **P. Clark di**  
Aires, ARG)

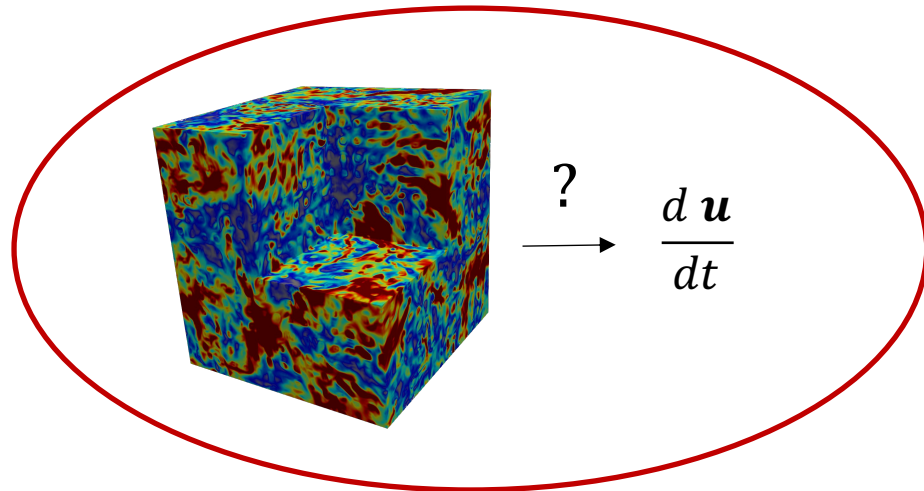


**TOR VERGATA**  
UNIVERSITY OF ROME

# Classifying Turbulent Environments via Machine Learning



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Can we improve our data-analysis capability to refine our physical knowledge of complex systems?

**Michele Buzzicotti**

Dept. Physics & INFN, University of Rome Tor Vergata

[michele.buzzicotti@roma2.infn.it](mailto:michele.buzzicotti@roma2.infn.it)

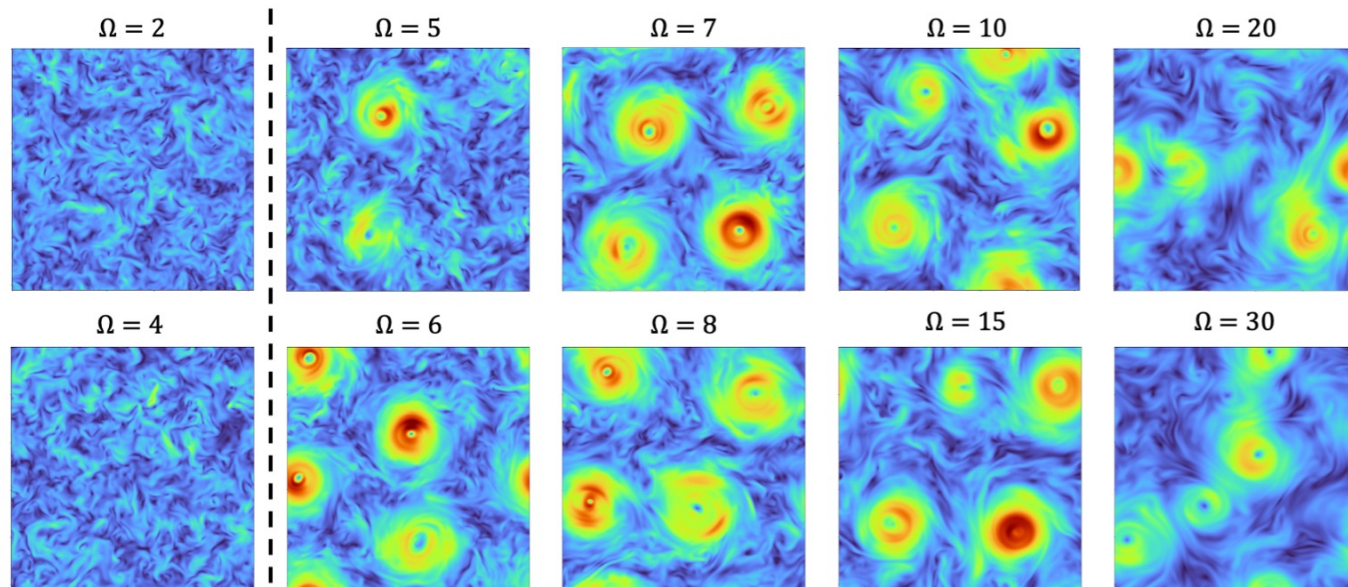
**CREDITS:** L. Biferale (Uni. Tor Vergata, IT),  
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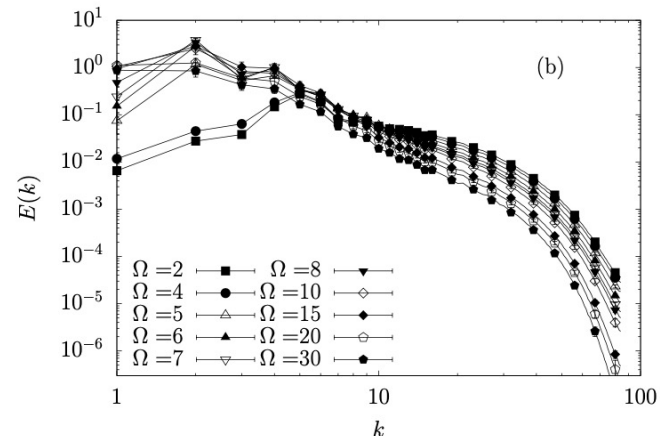
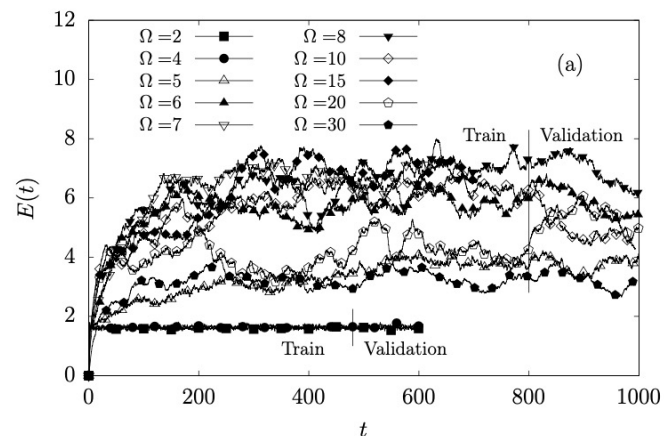
# Problem: Inferring the rotation rate

$$\partial_t \mathbf{v} + \mathbf{v} \cdot \partial_x \mathbf{v} + \partial_x P - \nu \Delta \mathbf{v} = 2 \mathbf{v} \times \boldsymbol{\Omega} + \mathbf{f}$$

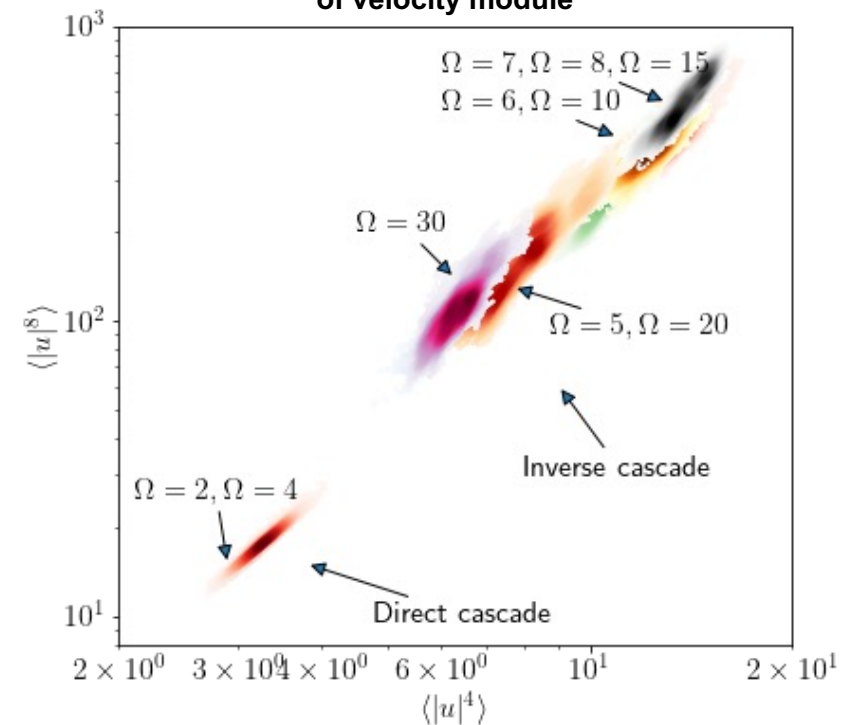


Direct

Inverse



Scatterplot of 8<sup>th</sup> vs 4<sup>th</sup> order moments of velocity module



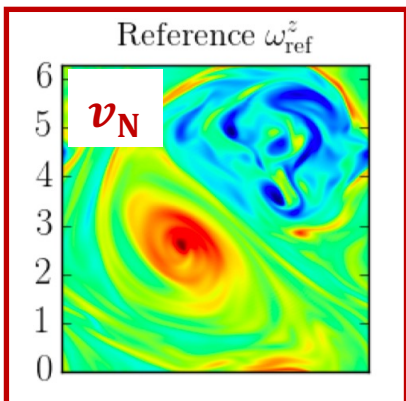
How can we extract useful information from one single velocity plane?

-] Alexakis, A., & Biferale, L. (2018). Cascades and transitions in turbulent flows. *Physics Reports*, 767, 1-101.

-] Di Leoni, P. Clark, Alexandros Alexakis, L. Biferale, and MB. "Phase transitions and flux-loop metastable states in rotating turbulence." *Physical Review Fluids* 5, no. 10 (2020): 104603.

# NUDGING: AN EQUATION-INFORMED TOOL TO INFER THE PHYSICS

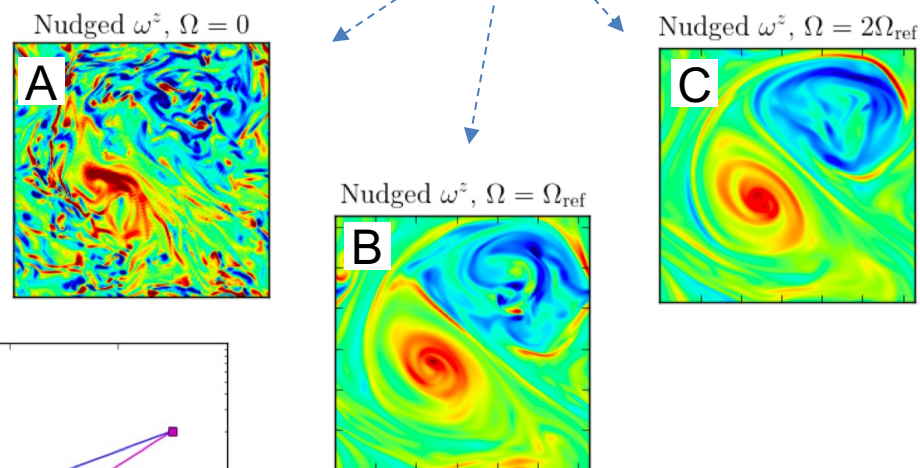
Reference DNS:



Nudging Simulation:

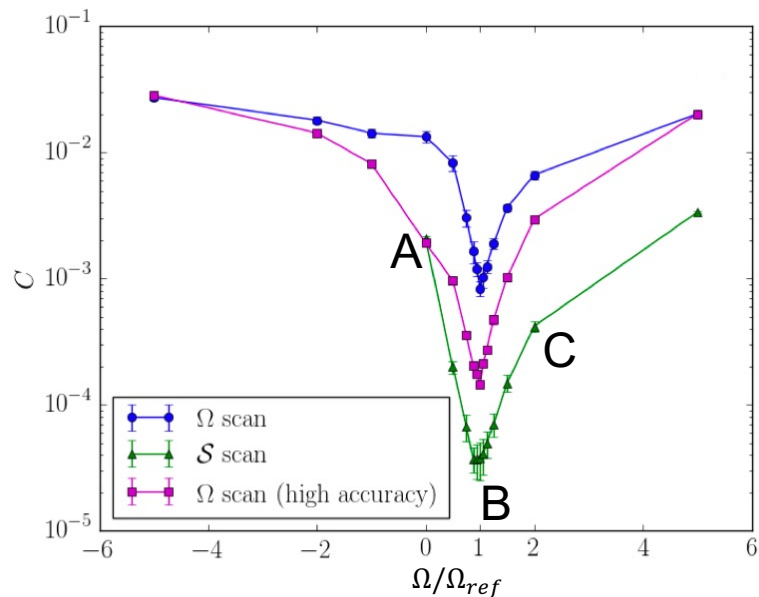
$$\partial_t \mathbf{v} + \mathbf{v} \cdot \partial_x \mathbf{v} + \partial_x P - \nu \Delta \mathbf{v} = 2 \mathbf{v} \times \boldsymbol{\Omega} + \mathbf{f} - N(\mathbf{v}_N - \mathbf{v})$$

DNS with the addition of a drag term against partial field measurements



$$E_{\Delta}(k) = \int_{|\mathbf{k}|=k} |\hat{u}(\mathbf{k}) - \hat{u}_N(\mathbf{k})|^2 d\mathbf{k}$$

$$C = \int_0^{k_c} E_{\Delta}(k) dk$$



Shows strong sensitivity to the physical parameter used in the nudged simulation

# NUDGING: TO OPTIMIZE SUBGRID SCALE MODELS

Nudging the Large Eddy Simulation:

$$\partial_t \tilde{\mathbf{v}} + \tilde{\mathbf{v}} \cdot \nabla \tilde{\mathbf{v}} = -\nabla \tilde{p} + \nu \Delta \tilde{\mathbf{v}} - \nabla \cdot \boldsymbol{\tau} + \mathbf{f} - N(\tilde{\mathbf{v}}_N - \tilde{\mathbf{v}})$$

$$\tilde{v}_i = \mathcal{F}(v_i) \quad \tilde{p} = \mathcal{F}(p) \quad \tau_{ij} = \mathcal{F}(v_i v_j) - \mathcal{F}(v_i) \mathcal{F}(v_j)$$

Filtered fields

Smagorinsky closure

$-2\nu_S S_{ij}$ , with:

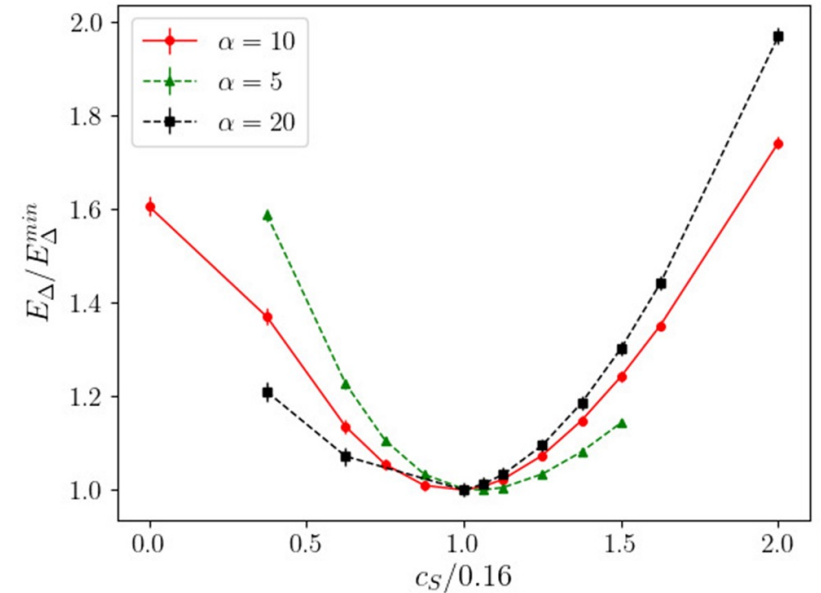
$$S_{ij} = \frac{1}{2} (\partial_j \tilde{v}_i + \partial_i \tilde{v}_j) \quad \nu_S = (c_S \Delta)^2 \sqrt{2 S_{kl} S_{kl}}$$

Is there an optimal value of  $c_S$  ?

We can optimize the Smagorinsky free-parameter, by minimizing the error between the reference DNS and the nudged LES:

$$E_\Delta = \int_0^{k_c} \int_{|\mathbf{k}|=k} |\hat{\mathbf{u}}(\mathbf{k}) - \hat{\mathbf{u}}_N(\mathbf{k})|^2 d\mathbf{k}$$

Filtered solution from fully resolved DNS:



$c_S = 0.16$  is found to minimize the average relative error.

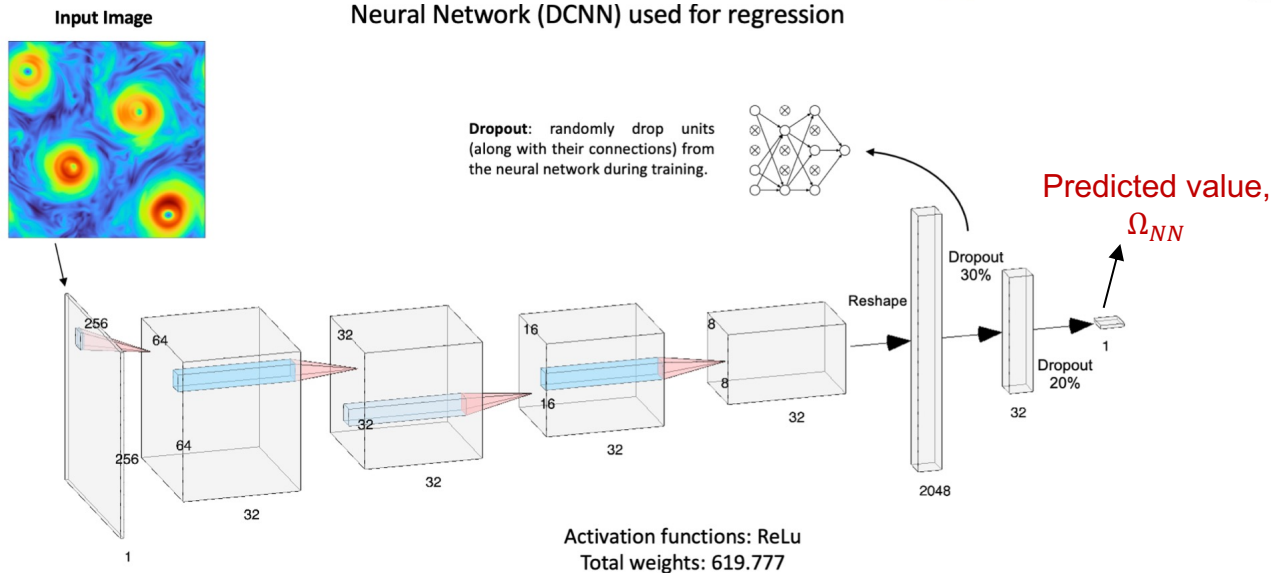
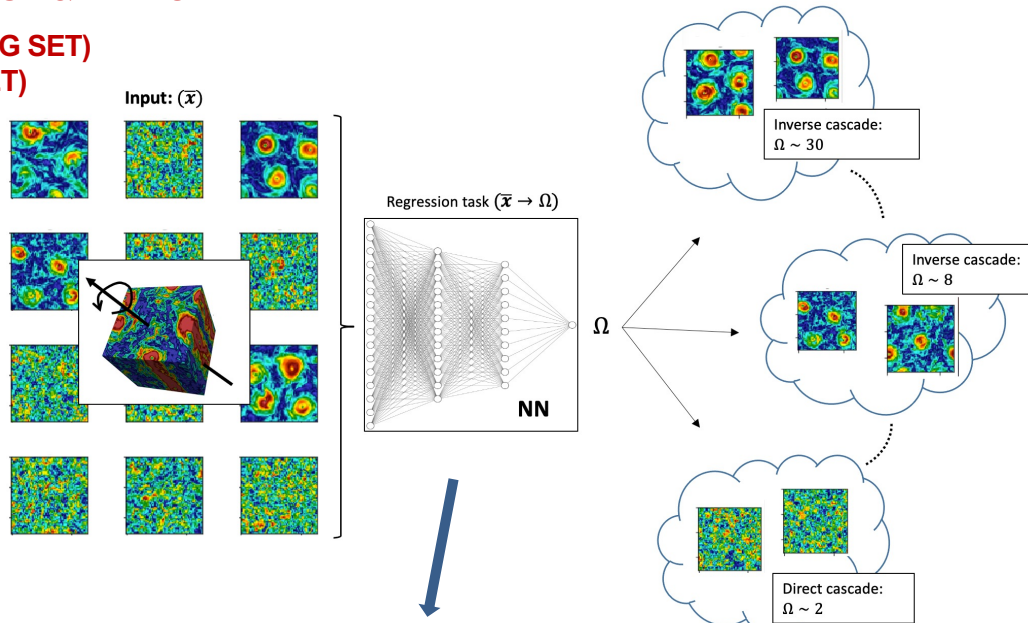
Important result to optimize new model and/or modeling in different setups (i.e. non-homogenous flows)



# MACHINE LEARNING: A DATA-DRIVEN TOOL TO INFER THE PHYSICS

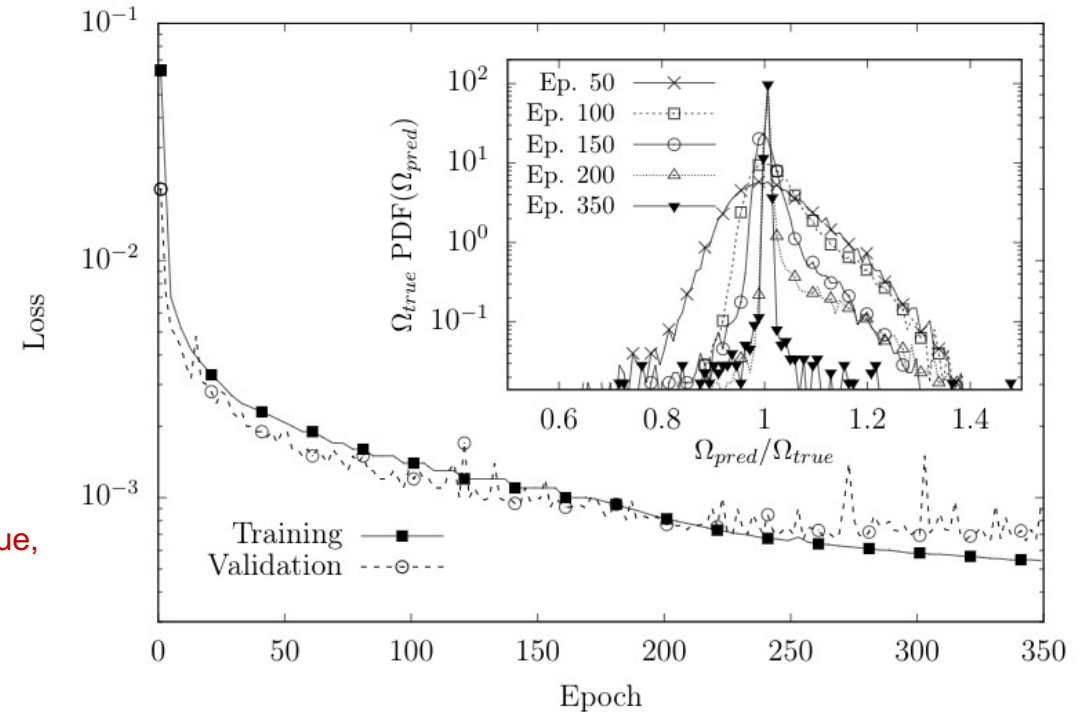
## PROBLEM SETUP & DATASET

- **400k** 2D planes (TRAINING SET)
- **100k** 2D planes (TEST SET)
- **10**  $\Omega$  values
- **Velocity module**
- **No time information**



Loss Function for the  $\Omega$  regression task:

$$\mathcal{L} = \mathbb{E}\{(\Omega_{true} - \Omega_{NN})^2\}$$

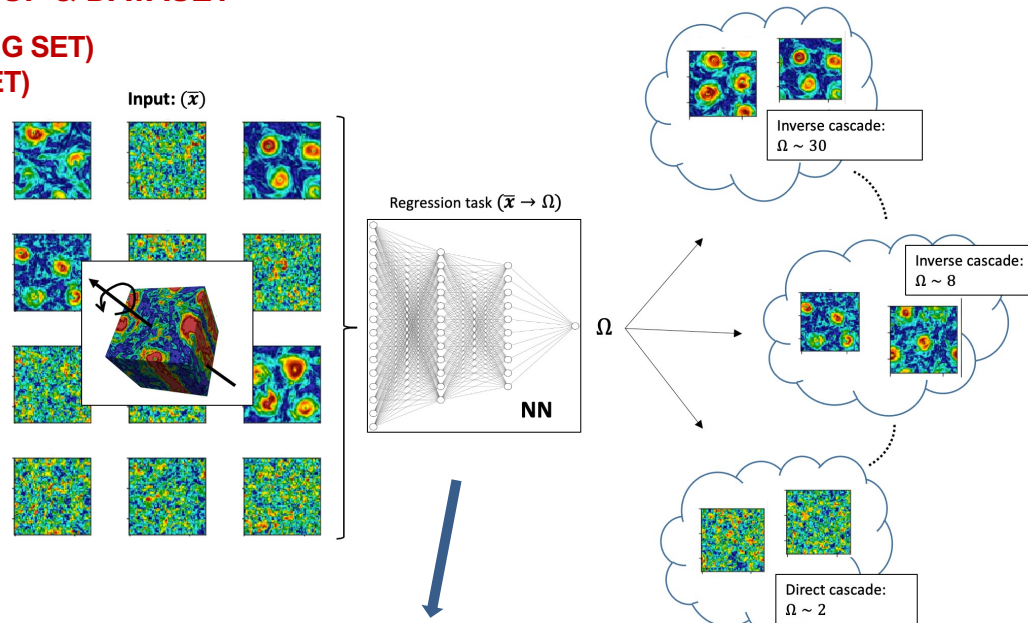


**Training details:** Minibatch 256 planes, Adam optimizer with Nesterov momentum, learning rate  $10^{-5}$ , ReLu activation function

# MACHINE LEARNING: A DATA-DRIVEN TOOL TO INFER THE PHYSICS

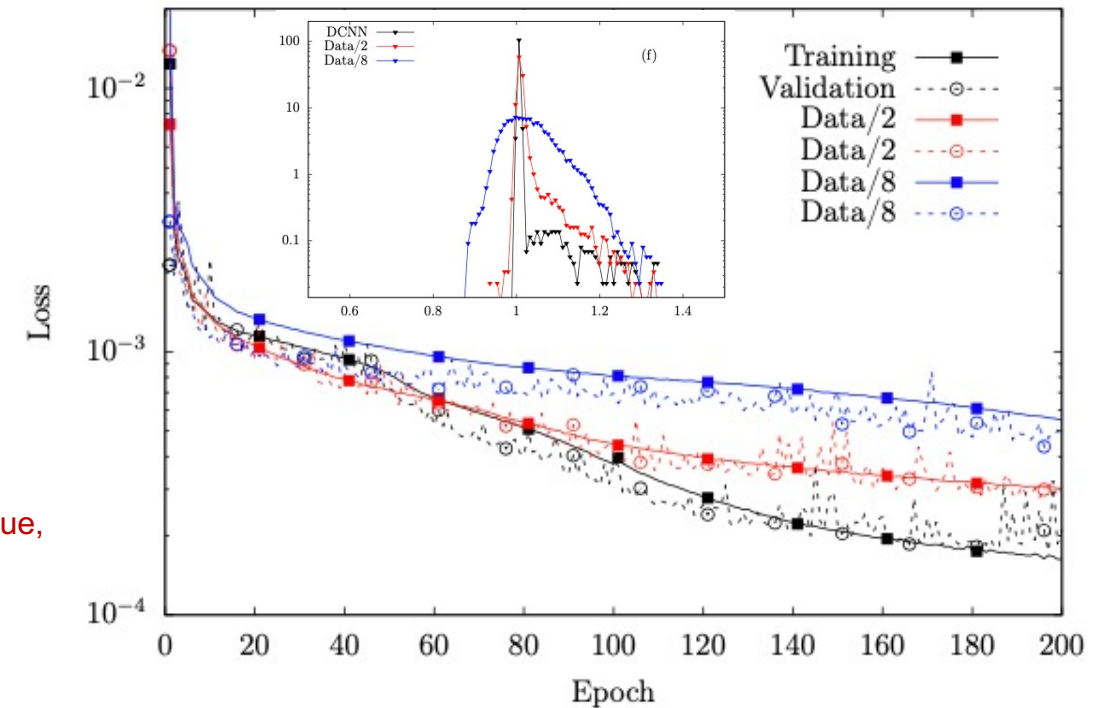
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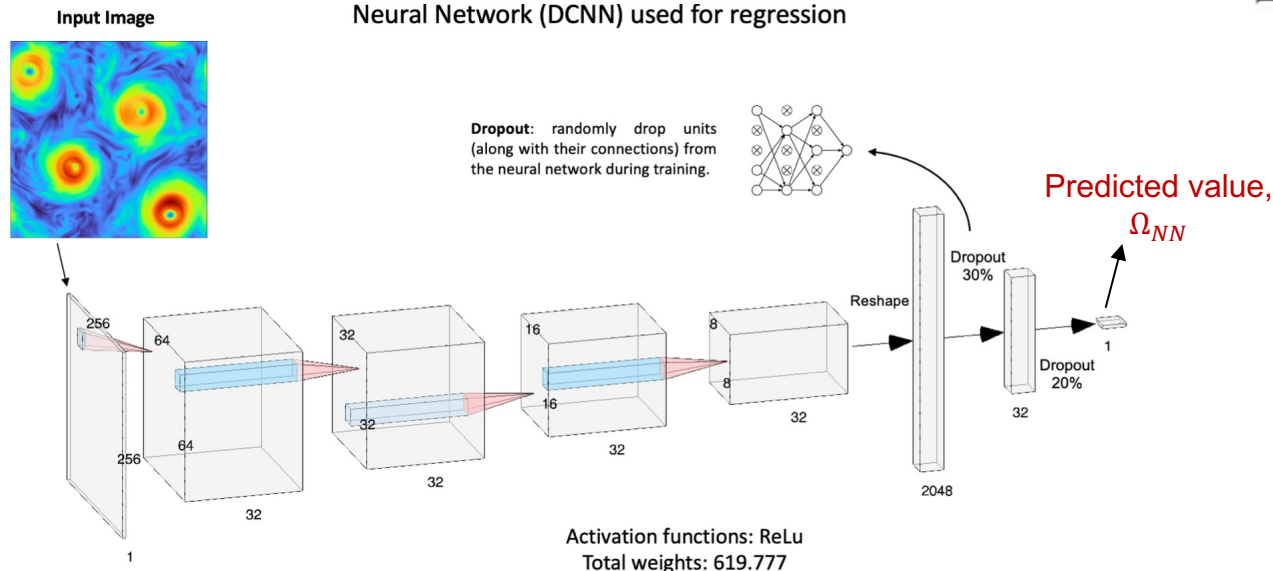


Loss Function for the  $\Omega$  regression task:

$$\mathcal{L} = \mathbb{E}\{(\Omega_{true} - \Omega_{NN})^2\}$$



Neural Network (DCNN) used for regression



**Training details:** Minibatch 256 planes, Adam optimizer with Nesterov momentum, learning rate  $10^{-5}$ , ReLu activation function



# DATA-DRIVEN BAYESIAN INFERENCE

$$\Omega_{Bay}(\mathcal{O}) = \max_{\Omega_i} P(\Omega_i|\mathcal{O})$$

We measure **mean squared velocity** and **mean squared velocity gradients** :

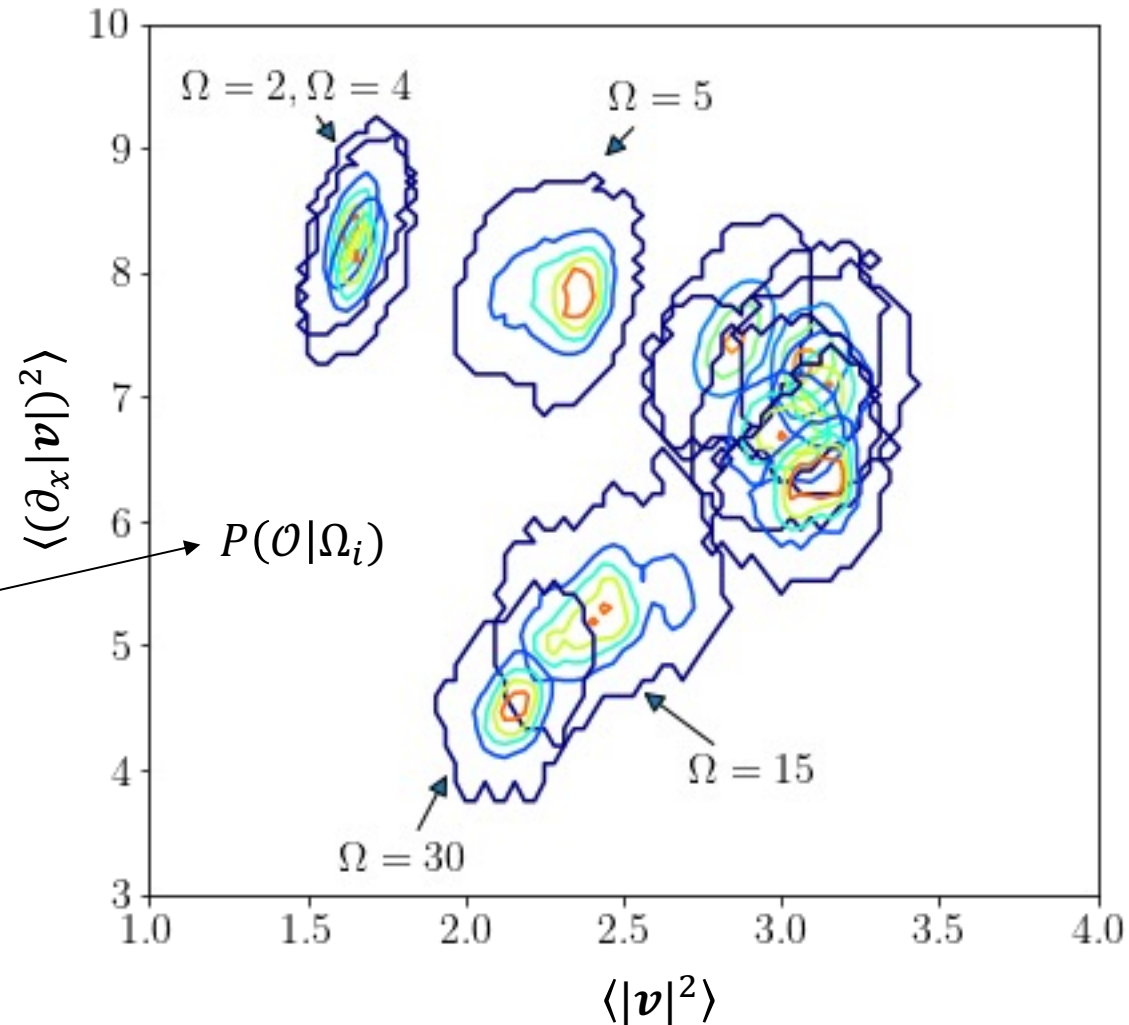
$$\mathcal{O} = (\langle |\mathbf{v}|^2 \rangle, \langle (\partial_x |\mathbf{v}|)^2 \rangle)$$

$\langle \dots \rangle$  mean on space, over the 2D plane

We can obtain the joint probability using Bayes Theorem:

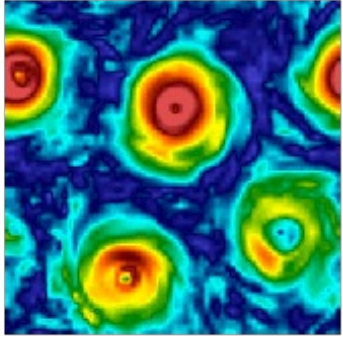
$$P(\Omega_i|\mathcal{O}) = \frac{P(\mathcal{O}|\Omega_i)P(\Omega_i)}{P(\mathcal{O})} = \frac{P(\mathcal{O}|\Omega_i)P(\Omega_i)}{\sum_i P(\mathcal{O}|\Omega_i)P(\Omega_i)}$$

Joint-PDF of **mean squared velocity** and **mean squared velocity gradients**  
(estimated over the 400k planes of the training set)

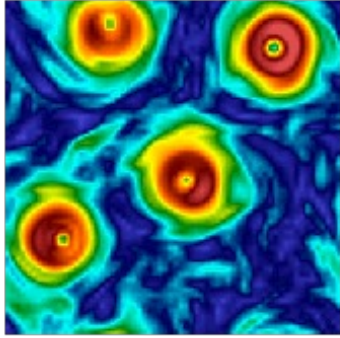


# comparison: BAYESIAN INFERENCE vs ML

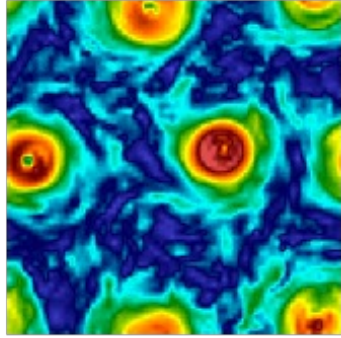
$\Omega = 7$ ; NN = 8.05; Bay = 10.14



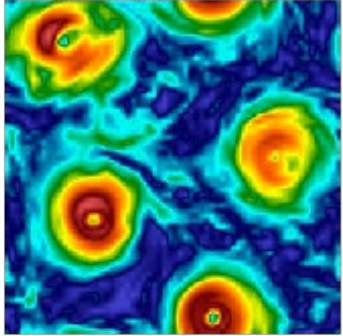
$\Omega = 15$ ; NN = 14.99; Bay = 9.77



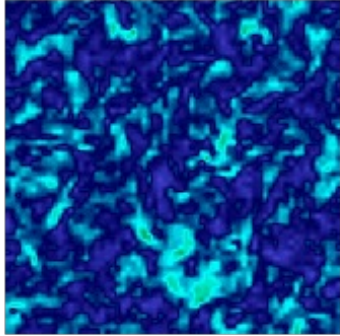
$\Omega = 6$ ; NN = 6.00; Bay = 7.74



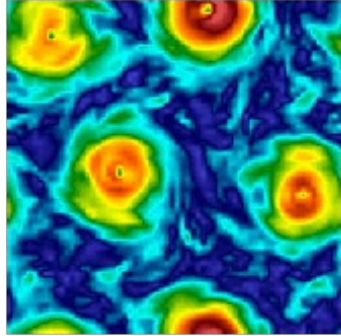
$\Omega = 8$ ; NN = 7.54; Bay = 10.28



$\Omega = 2$ ; NN = 2.52; Bay = 3.09



$\Omega = 7$ ; NN = 7.23; Bay = 9.43



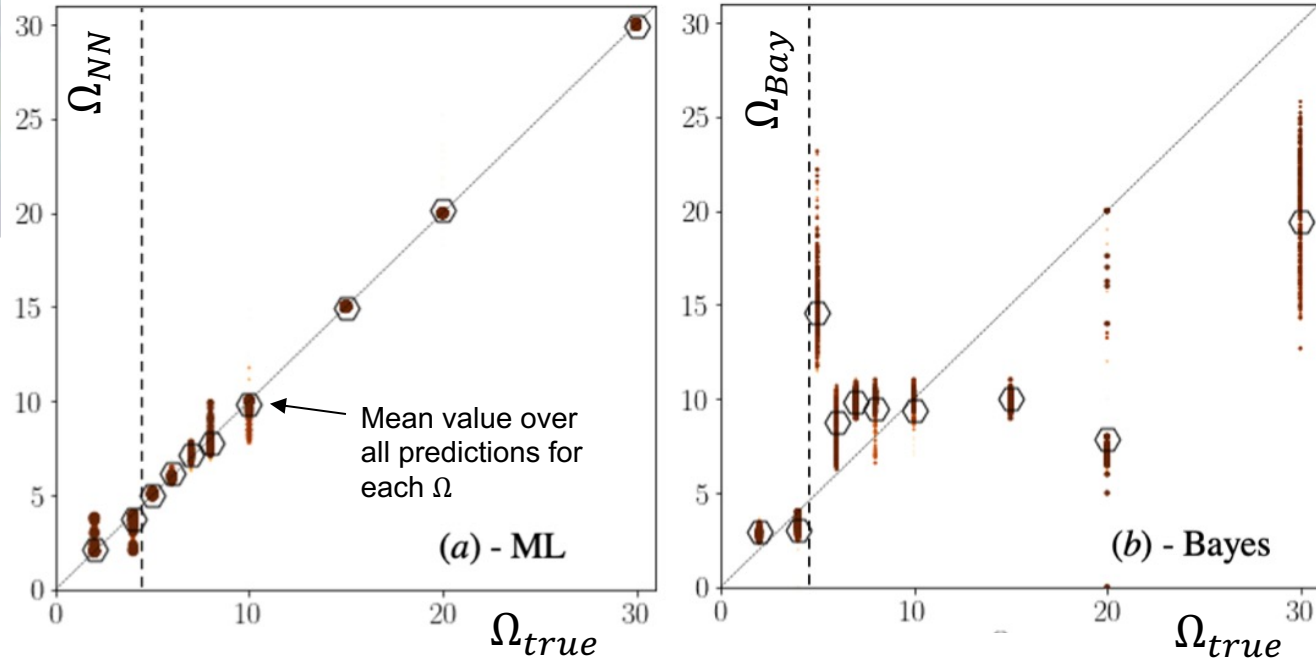
Examples of  $\Omega$  inferring by Neural Network and Bayesian Inference

## Scatterplot of Prediction vs True $\Omega$ values

Results obtained on the TEST SET (100k planes)

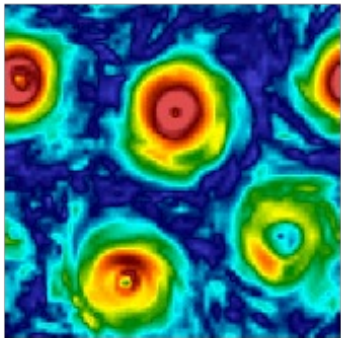
Bayes infers on: velocity square module

$$P(\Omega_i | \langle |v|^2 \rangle)$$

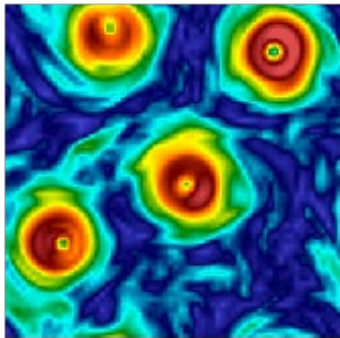


# comparison: BAYESIAN INFERENCE vs ML

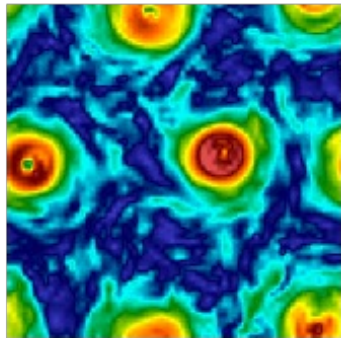
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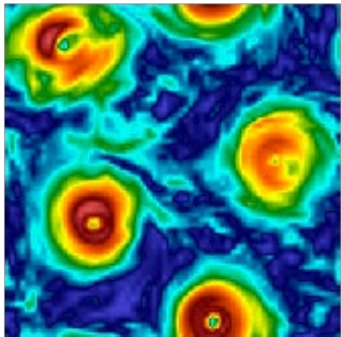
$\Omega = 15$ ; NN = 14.99; Bay = 9.77



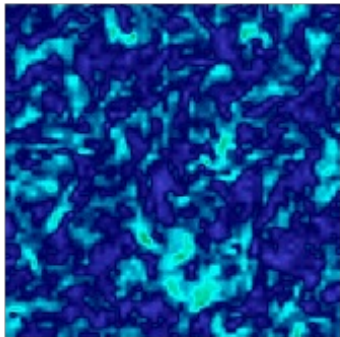
$\Omega = 6$ ; NN = 6.00; Bay = 7.74



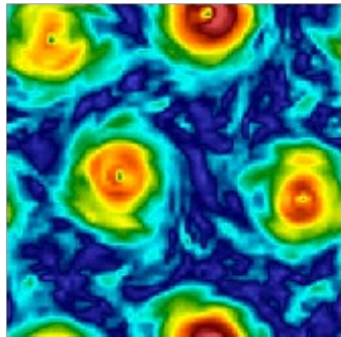
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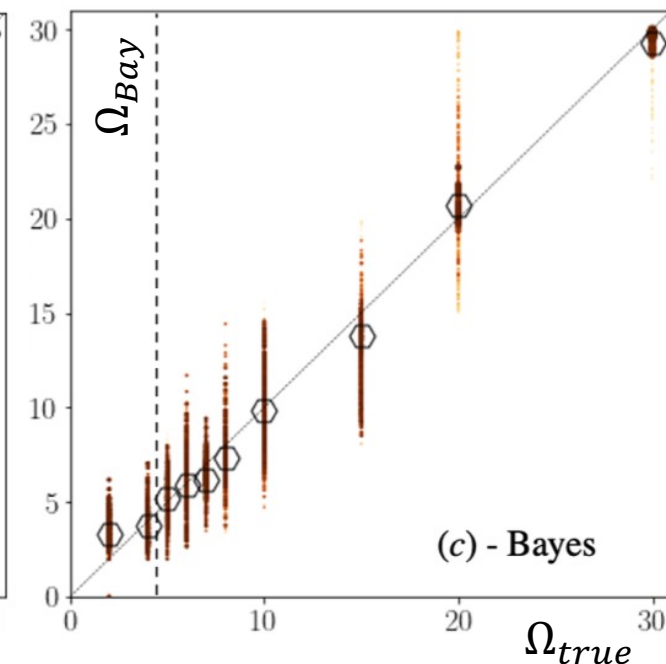
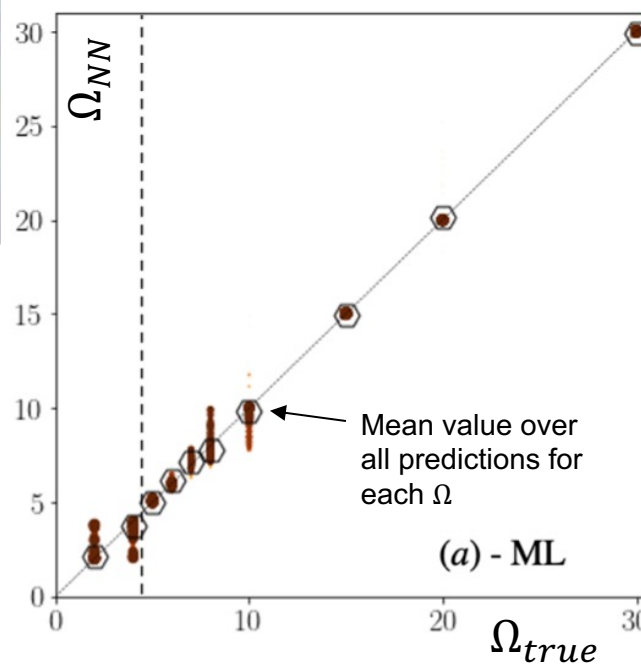
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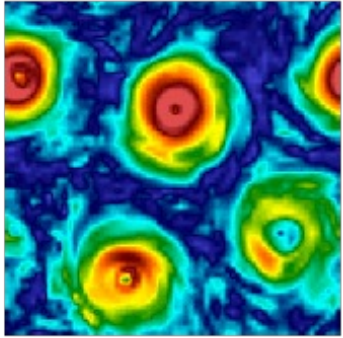
$$P(\Omega_i | \langle (\partial_x |v|)^2 \rangle)$$



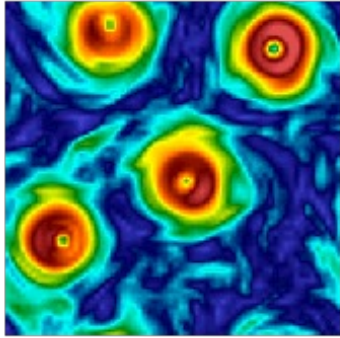


# comparison: BAYESIAN INFERENCE vs ML

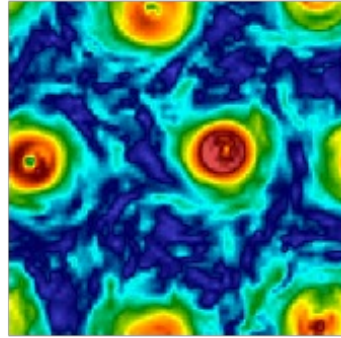
$\Omega = 7$ ; NN = 8.05; Bay = 10.14



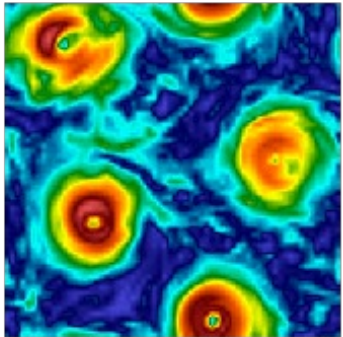
$\Omega = 15$ ; NN = 14.99; Bay = 9.77



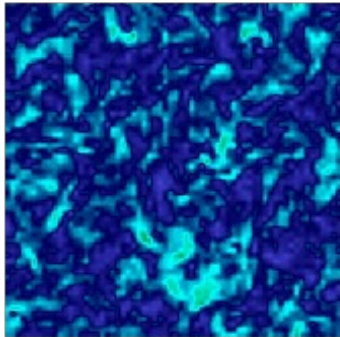
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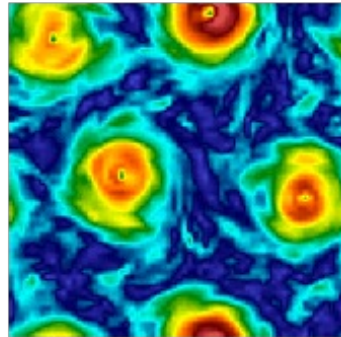
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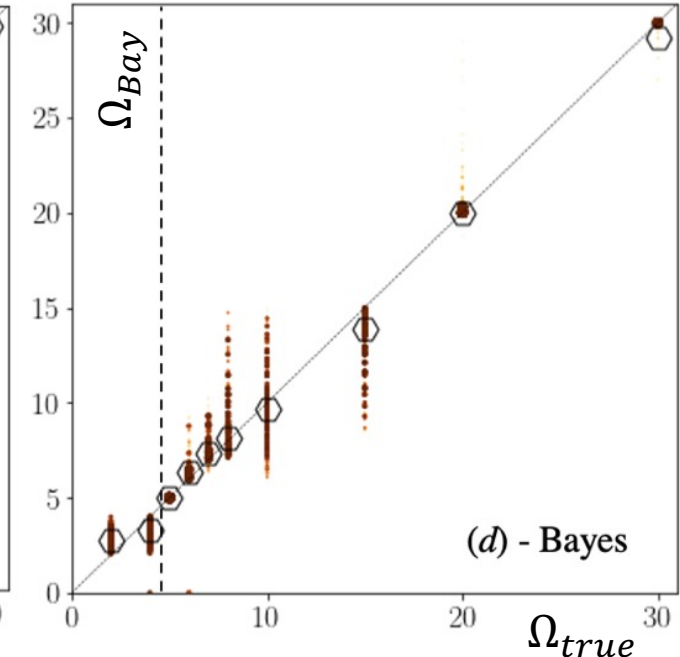
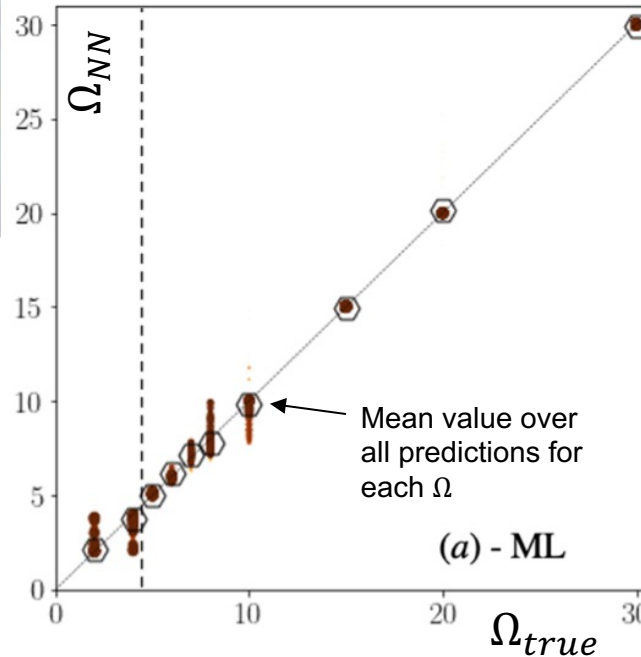
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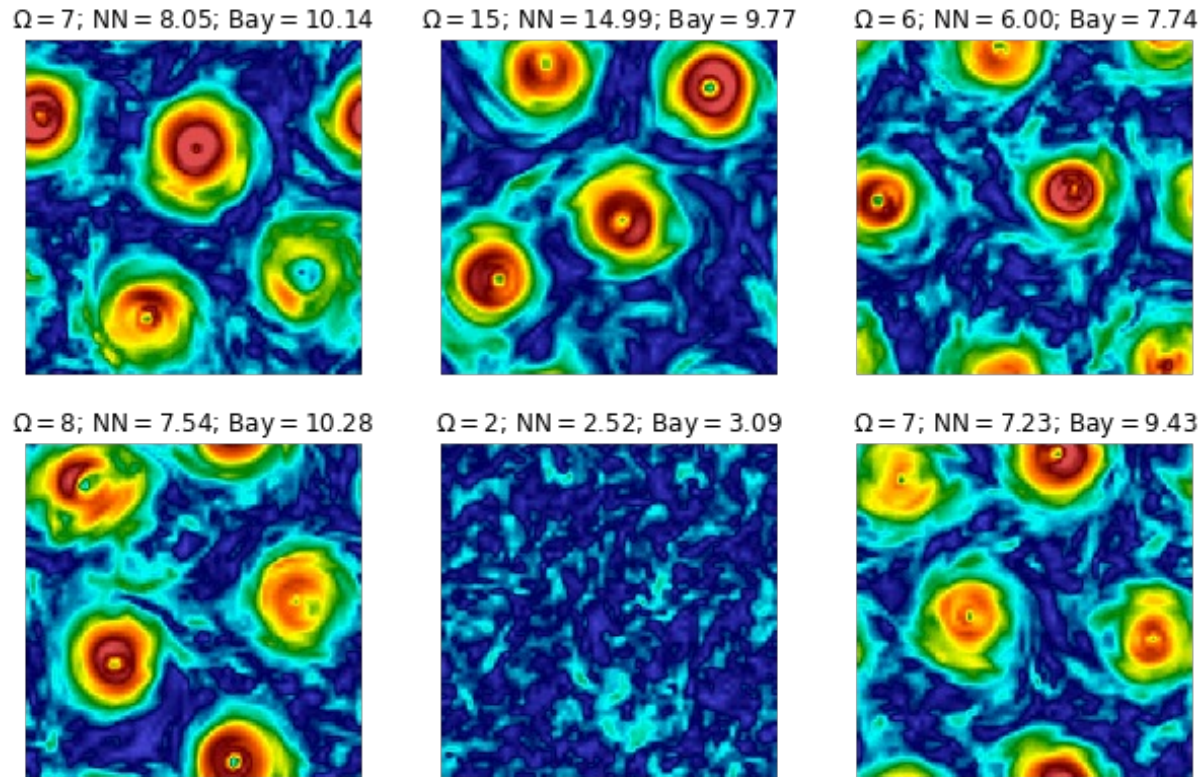
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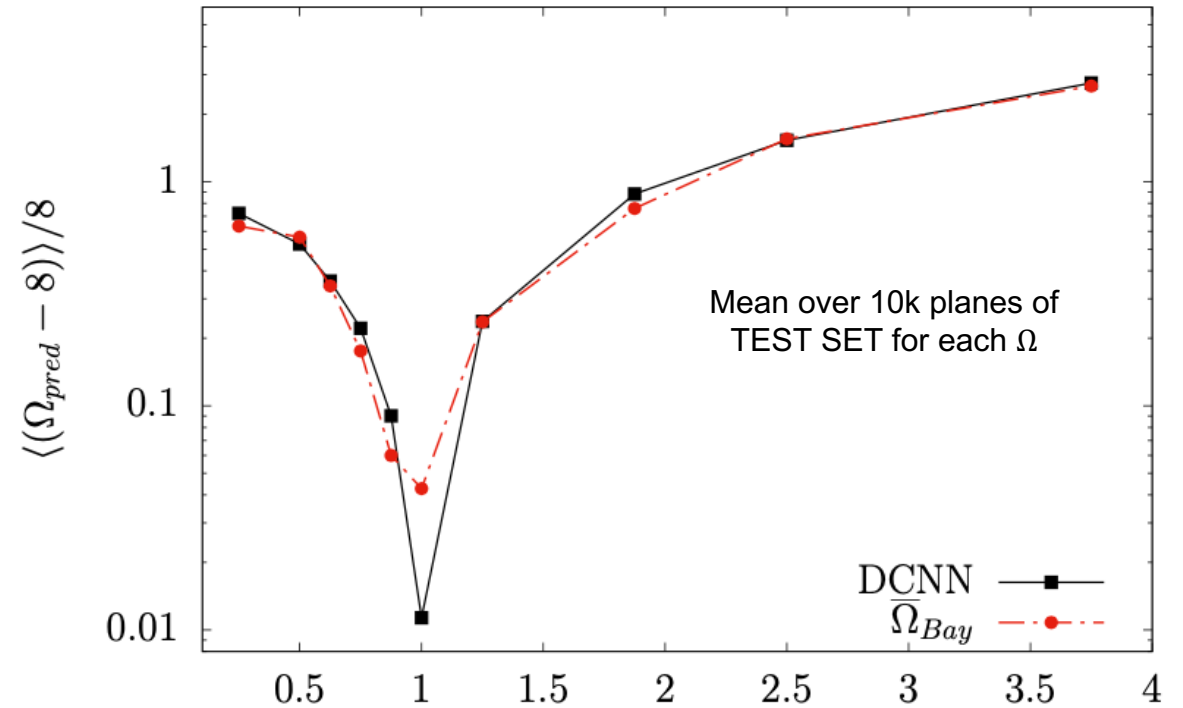


# comparison: BAYESIAN INFERENCE vs ML



Examples of  $\Omega$  inferring by Neural Network and Bayesian Inference

## Sensitivity of Data-Driven Tools

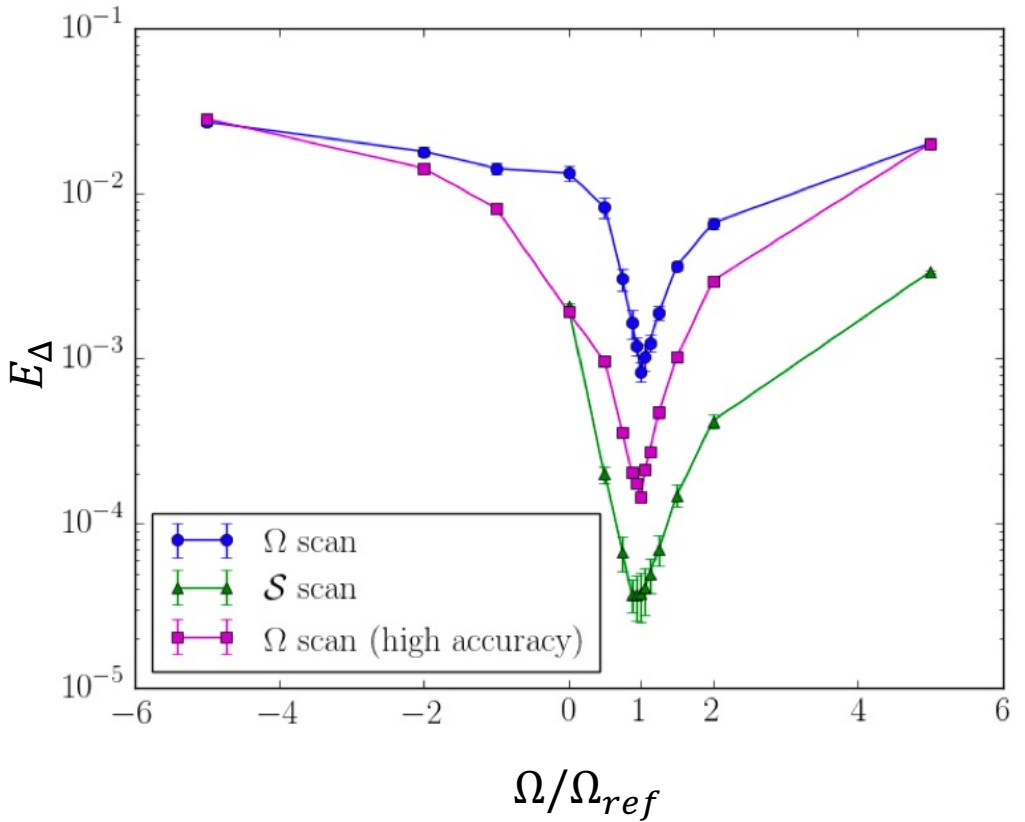


$\partial_t \mathbf{v} + \mathbf{v} \cdot \partial_x \mathbf{v} + \partial_x P - \nu \Delta \mathbf{v} = 2 \mathbf{v} \times \Omega \hat{\mathbf{z}} + \mathbf{f}$

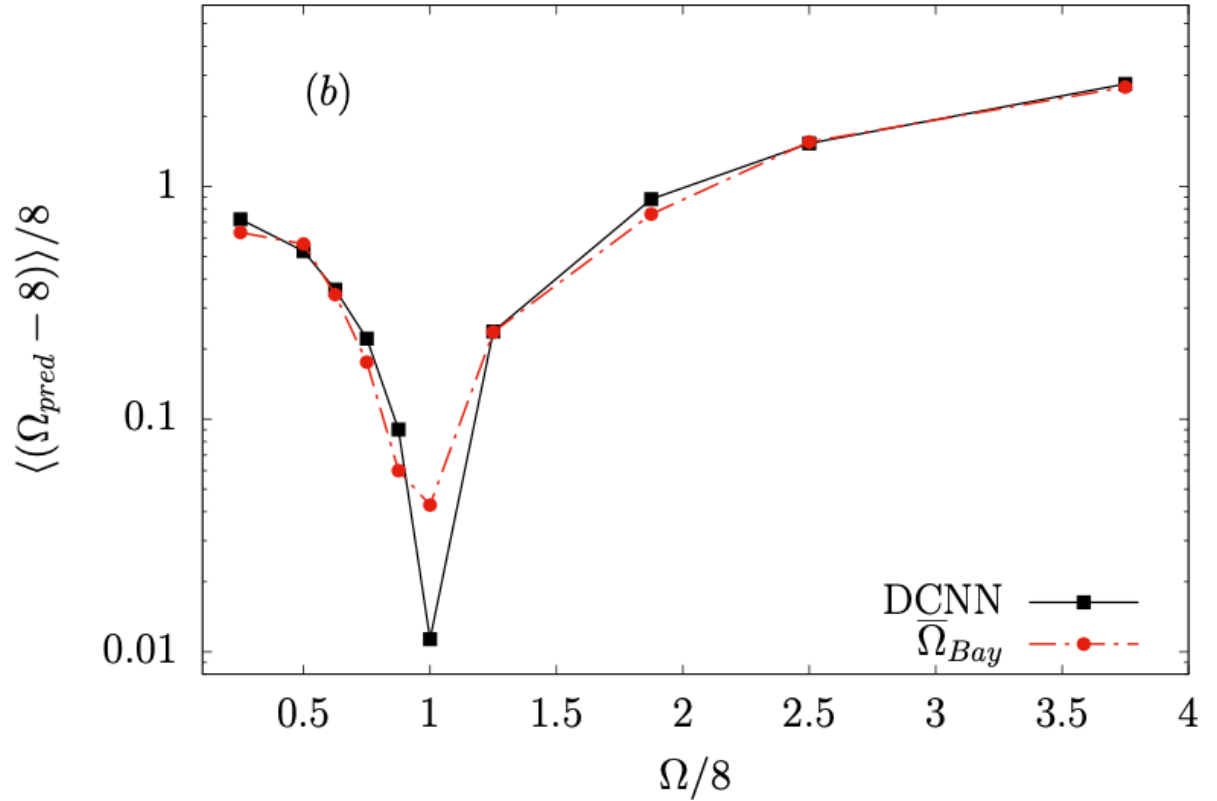
$\nearrow \Omega/8$

# Contributions

## NUDGING: EQUATION-INFORMED



## DATA-DRIVEN TOOLS



- + Strong Sensitivity to the physical parameter
- + No need of Ensemble/Training Dataset
- It requires complete knowledge of the Equations
- Heavy in computation – it requires DNS

- + Strong Sensitivity to the physical parameter
- + No need of Eq. of Motion
- + Fast in computation after the training
- Need of large Training Dataset



# References

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  - MB, Bonaccorso, Clark Di Leoni & Biferale. **Phys. Rev. Fluids 6, 050503 (2021)**.  
Reconstruction of turbulent data with deep generative models for semantic inpainting from TURB-Rot database.
    - Biferale, Bonaccorso, MB & Clark di Leoni. **arXiv:2006.07469 (2020)**.  
TURB-Rot. A large database of 3d and 2d snapshots from turbulent rotating flows.
- Biferale, Bonaccorso, MB, Clark Di Leoni & Gustavsson. **Chaos: An Interdisciplinary Journal of Nonlinear Science. 2019 Oct 24;29(10):103138**.  
Zermelo's problem: Optimal point-to-point navigation in 2D turbulent flows using reinforcement learning.
- MB, Biferale, Bonaccorso, Clark Di Leoni & Gustavsson. **Springer, Cham, (2021)**. Optimal Control of Point-to-Point Navigation in Turbulent Time Dependent Flows Using Reinforcement Learning.
  - Clark Di Leoni, Mazzino, Biferale. **Phys. Rev. Fluids 3, 104604, (2018)**. Inferring flow parameters and turbulent configuration with physics-informed data-assimilation and spectral nudging.
- Clark Di Leoni, Mazzino, Biferale. **Phys. Rev. X 10.1, 011023, (2020)**. Synchronization to big-data: nudging the Navier-Stokes equations for data assimilation of turbulent flows.
  - Colabrese, Gustavsson, Celani, Biferale. **Phys. Rev. Fluids 3, 084301, (2018)**. Smart Inertial Particles.
- Colabrese, Gustavsson, Celani, Biferale. **Phys. Rev. Letters 118 (15), 158004, (2017)**. Flow navigation by smart microswimmers via reinforcement learning.

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TURB-ROT. A LARGE DATABASE OF 3D AND 2D SNAPSHOTS  
FROM TURBULENT ROTATING FLOWS

---

A PREPRINT

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<p><b>M. Buzzicotti</b> Dept. Physics and INFN University of Rome Tor Vergata, Italy. michele.buzzicotti@roma2.infn.it</p>	<p><b>P. Clark Di Leoni</b> Department of Mechanical Engineering, Johns Hopkins University, Baltimore, USA. pato@jhu.edu</p>



Smart-Turb Datasets Organizations Help About

**Guide for users**

What is Smart-TURB? It is a brand new software infrastructure (born June 2020) for the research community working on turbulence and complex flows with particular emphasis to collect/standardize and preserve huge dataset for big-data and Machine Learning approaches to fluid mechanics in general and turbulence, in particular. It is an easily accessible web platform for high quality data. Its main goal is to host, standardize and manage a large collection of heterogeneous datasets from different sources.

<https://smart-turb.roma2.infn.it/>

Please contact the administrator for infos about how to upload your dataset. We start by deploying a first dataset made of 2d and 3d turbulent configurations under rotation TURB-Rot. More will come.

Search for datasets

<p><b>1</b> Datasets</p> <p>TURB-Rot A large database of 3d and 2d snapshots from turbulent rotating</p>	<p><b>2</b> Organizations</p> <p>web_admin web_admin group 1 member</p>
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